

Research Paper

Comparison of Various Prediction Model for Biodiesel Cetane Number using Cascade-Forward Neural Network

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Abstract

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Cetane number (CN) is one of the important fuel properties of diesel fuels. It is a measurement of the ignition quality of diesel fuel. Numerous studies have been published to predict the CN of biodiesels. More recently, the utilization of soft computing methods such as artificial neural networks (ANN) has received considerable attention as a prediction tool. However, most studies in the use of ANN for estimating the CN of biodiesels have only used one algorithm to train a small number of datasets. This study aims to predict the CN of 63 biodiesels based on the fatty acid methyl esters (FAME) composition by developing an ANN model that was trained with 10 different algorithms. To the best of our knowledge, this is the first study to predict the CN of biodiesels using numerous ANN training algorithms utilizing sizeable datasets. Results revealed that the ANN model trained with Levenberg-Marquardt gave the highest prediction accuracy. LM algorithm successfully predicted the CN of biodiesels with the highest correlation and determination coefficient ($R = 0.9615$, $R^2 = 0.9245$) as well as the lowest errors ($MAD = 2.0804$, $RMSE = 3.1541$, and $MAPE = 4.2971$). Hence, the Cascade neural network trained with the LM algorithm could be considered a promising alternative to the empirical correlations for predicting biodiesel's CN.

Keywords: Biodiesel; Cetane number; Cascade neural network; Artificial neural network; Fuel properties; FAME

1. Introduction

Despite the emerging trend of electric vehicles [1], [2], the internal combustion engine (ICE) remains the most dominant power engine due to its mature technology [3]–[6]. However, it is important to note that ICE needs fuel from fossil hydrocarbons that are rare and not available in large amounts, making it costly to produce [7].

Petroleum-based fuel is commonly known for its derivation products such as gasoline, diesel, and jet fuel [8]. Regrettably, fossil fuel is still dominating the transportation sectors worldwide as the primary energy source since it is suitable for most engine applications [9].

Furthermore, the increasing population, expanding urbanization, and better living



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standards have raised global energy consumption [10]. On the contrary, fossil fuel reserves have been diminishing more and more in the last two decades. Environment concerns and anxiety over the decreasing fossil fuel have thus made alternative fuel to be a feasible option to meet future energy demands [11]–[13].

The esters from vegetable oil can be used as the energy source for diesel engines and, due to its natural ingredient, is often referred to as biodiesel [14]. Biodiesel is among the alternative fuel that has gained popularity globally [15]. The use of such fuel is being encouraged by many countries to replace conventional diesel fuel with fossil. The main objective is to decrease dependency on foreign oil as well as to reduce the greenhouse effect. Biodiesel is believed to be a non-toxic biodegradable fuel that can be used in diesel engines without major modification. In addition, fuel derived from biodiesel processes has emerged as renewable and non-toxic compared to conventional diesel fuel. Neither net carbon dioxide nor sulfur is released from such fuel, emitting fewer pollutants emissions to the environment.

During the late 90s, soybean oil was primarily used in the US, being the only oil that is sufficiently available to the national demand. Yet, the production cost to produce this edible vegetable oil was expensive. As a result, it was only used in cases of the serious scarcity of petroleum diesel fuel. To be commercially visible, it is important to reduce the cost of the feedstock. One possible way to make it more affordable is to use feedstocks that are less expensive. Used oils, greases, and animal fats are good sources of economical biodiesel.

Many, however, are concerned with the issue of increasing food and water prices if biodiesel is produced from edible sources. Hence, second-generation biofuels are developed, being made from waste materials. Waste cooking oil, for example, is abundant in most parts of the world. In fact, biodiesel from used cooking oil has been produced commercially in some countries. Non-edible vegetable oils are gaining popularity as promising substitutions for conventional edible food crops. With the enormous demand for edible oil as a food source, the deploying of such non-edible plant oils plays an important role to solve the food vs fuel dilemma.

Low-cost sources such as oils from restaurants have been widely used recently with regard to edible feedstocks. Nevertheless, producing produce fuel-grade biodiesel from this low-cost oil is far more difficult as they encompass a high level of free fatty acids. Various studies have indicated that the use of waste cooking oil biodiesel reduces a considerable amount of particulate matter, CO, and total hydrocarbon emissions with no efficiency loss in several types of diesel engines in comparison to conventional diesel fuel. Some studies have also shown that NO_x emissions rise slightly. Note that sharp rises in both NO_x and PM emissions may occur when cooking oil biodiesel fuel is used.

Many researchers have pointed out that biodiesel's properties bear a close resemblance to those of petroleum-based diesel fuel. The studies of biodiesel in optimization models have been analyzed and discussed by numerous researchers [16]–[18]. As a result, biodiesel can be widely used in diesel engines with little or no alteration. Some considerations, however, need to be addressed. Take flash point properties for example. The flash point is a substantial safety measure of fuel flammability. Biodiesel tends to have flash point that is two times higher than conventional diesel fuel. This, fortunately, can be solved by adding residual alcohol to lower its flash point. Another fuel property to be considered is viscosity. It affects the volume flow and injection spray characteristics of an engine. Biodiesel kinematic viscosity is known to be higher than that of diesel fuel. Consequently, biodiesel at low temperatures can be very viscous or even solidified, compromising the mechanical integrity of the injection pump drive system. Nevertheless, biodiesel still provides superior advantages, namely, relatively higher CN, no aromatics, and contains 10% to 11% oxygen by weight. These, consequently, decrease the emissions of carbon monoxide (CO), hydrocarbons (HC), and particulate matter (PM).

CN, in particular, is an indicator of the ignition quality of diesel fuel. The greater the number, the better the fuel burns. The CN is comparable to the octane number for gasoline fuel as a measurement of combustion quality. The major difference between cetane and octane numbers is that the octane number measures the ability of a fuel to resist unwanted initial ignition caused by compression so that the fuel only ignites from a

spark plug. By contrast, the CN measures the ignition delay of a fuel. Therefore, a higher-performance gasoline engine needs fuel with a greater octane number, whereas a high-performance diesel vehicle needs fuel with a greater CN to enable fast ignition and avoid incomplete combustion.

2. Novelty of the Study

Regardless of the feedstock sources, it is important to remember that fuel properties of biodiesel such as density, kinematic viscosity, and CN should meet certain standards like ASTM. As most fuel properties are significantly reliant on the compositions of the feedstock, it is therefore different feedstock will have different fuel properties.

Many previous studies have been published to estimate biodiesel CN. More recently, the utilization of soft computing methods such as artificial neural networks (ANN) has received considerable attention as a prediction tool [19]–[21]. However, most studies in the use of ANN for estimating the CN of biodiesels have only used less algorithms to train small number of datasets. Hence, by greater number of data, it would give a better prediction of CN. In addition, this study proposed 10 different techniques (algorithm) to predict the CN.

The 10 proposed techniques are not the new approach in ANN. However, to compare many

techniques (more than 5) have not been considered yet previously in the literatures. Additionally, there was a lack of information on the best techniques. To find the best technique, many techniques shall be tested and compared.

This study aims to predict the CN of 63 biodiesels based on the fatty acid methyl esters (FAME) composition by developing an ANN model that was trained with 10 different algorithms as shown in Figure 1. To the best of our knowledge, this is the first study to predict the CN of biodiesel using numerous ANN training algorithms utilizing sizeable datasets.

3. Method

3.1. Data Gathering

Data from 63 biodiesel CNs along with their fatty acid methyl esters (FAME) composition have been gathered from previous studies [22]–[26] and are presented in Table 1. The dataset has values of CN ranging from 20.4 to 86.9.

3.2. Cascade Neural Network

Previous studies have noted the importance of artificial neural networks [27], [28]. However, numerous machine learnings have been studied for prediction models or other purposes, such as response surface method (RSM), surrogate model, and metamodeling.



Figure 1. Ten algorithms used in this study for cascade neural network

Table 1. FAME composition of different biodiesel sources

| Biodiesel | 12:00 | 14:00 | 16:00 | 16:01 | 18:00 | 18:01 | 18:02 | 18:03 | 20:01 | 22:01 | CN |
|--------------------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|--------------|-----------|
| Lauric | 100 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 61.4 |
| Myristic | 0 | 100 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 66.2 |
| Palmitic | 0 | 0 | 100 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 74.5 |
| Stearic | 0 | 0 | 0 | 0 | 100 | 0 | 0 | 0 | 0 | 0 | 86.9 |
| Oleic | 0 | 0 | 0 | 0 | 0 | 100 | 0 | 0 | 0 | 0 | 55 |
| Palmitoleic | 0 | 0 | 0 | 100 | 0 | 0 | 0 | 0 | 0 | 0 | 51 |
| Linoleic | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 0 | 0 | 0 | 42.2 |
| Erucic | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 76 |
| Eicosanoic | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 0 | 64.8 |
| Linolenic | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 100 | 0 | 0 | 20.4 |
| Soybean | 0 | 0.1 | 10.5 | 0.1 | 3.7 | 23.2 | 48.9 | 1.2 | 0.3 | 0.1 | 47.2 |
| Inedible tallow | 0.1 | 2.1 | 23.9 | 2.8 | 19.5 | 38.5 | 6.4 | 0.3 | 0.5 | 0.1 | 61.7 |
| Thevetia peruviana M. | 0 | 0 | 15.6 | 0 | 10.5 | 60.9 | 5.2 | 7.4 | 0 | 0 | 57.5 |
| Moringa oleifera Lam | 0 | 0 | 9.1 | 2.1 | 2.7 | 79.4 | 0.7 | 0.2 | 0 | 0 | 56.7 |
| Pongamia pinnata P. | 0 | 0 | 10.6 | 0 | 6.8 | 49.4 | 19 | 0 | 2.4 | 0 | 55.8 |
| Holoptelia integrifolia | 0 | 3.5 | 35.1 | 1.9 | 4.5 | 53.3 | 0 | 0 | 0 | 0 | 61.2 |
| Vallisneria spiralis L. | 0 | 0 | 7.2 | 0 | 14.4 | 35.3 | 40.4 | 0 | 0 | 0 | 50.3 |
| Aleurites moluccana | 0 | 0 | 5.5 | 0 | 6.7 | 10.5 | 48.5 | 28.5 | 0 | 0 | 34.2 |
| Euphorbia helioscopia L. | 2.8 | 5.5 | 9.9 | 0 | 1.1 | 15.8 | 22.1 | 42.7 | 0 | 0 | 34.2 |
| Garcinia morella D. | 0 | 0 | 0.7 | 0 | 46.4 | 49.5 | 0.9 | 0 | 0 | 0 | 63.5 |
| Satureja hortensis Linn | 0 | 0 | 0.4 | 0 | 0.4 | 12 | 18 | 62 | 0 | 0 | 25.5 |
| Actinodaphne angust. | 87.9 | 1.9 | 0.5 | 0 | 5.4 | 0 | 0 | 0 | 0 | 0 | 63.2 |
| Litsea glutinosa Robins | 96.3 | 0 | 0 | 0 | 0 | 2.3 | 0 | 0 | 0 | 0 | 64.8 |
| Neolitsea cassia Linn | 85.9 | 3.8 | 0 | 0 | 0 | 4 | 3.3 | 0 | 0 | 0 | 64 |
| Swietenia mahagoni J. | 0 | 0 | 9.5 | 0 | 18.4 | 56 | 0 | 16.1 | 0 | 0 | 52.3 |
| Argemone mexicana | 0 | 0.8 | 14.5 | 0 | 3.8 | 18.5 | 61.4 | 0 | 0 | 0 | 44.5 |
| Salvadora persica Linn | 19.6 | 54.5 | 19.6 | 0 | 0 | 5.4 | 0 | 0 | 0 | 0 | 67.5 |
| Madhuca butyracea M. | 0 | 0 | 66 | 0 | 3.5 | 27.5 | 3 | 0 | 0 | 0 | 65.3 |
| Rhus succedanea Linn | 0 | 0 | 25.4 | 0 | 0 | 46.8 | 27.8 | 0 | 0 | 0 | 52.2 |
| Basella rubra Linn | 0 | 0.4 | 19.7 | 0.4 | 6.5 | 50.3 | 21.6 | 1.1 | 0 | 0 | 54 |
| Corylus avellana | 0 | 3.2 | 3.1 | 0 | 2.6 | 88 | 2.9 | 0 | 0 | 0 | 54.5 |
| Jatropha curcas Linn | 0 | 1.4 | 15.6 | 0 | 9.7 | 40.8 | 32.1 | 0 | 0 | 0 | 52.3 |
| Croton tiglium Linn | 0 | 11 | 1.2 | 0 | 0.5 | 56 | 29 | 0 | 0 | 0 | 49.9 |
| Princeps utilis Royle | 0 | 1.8 | 15.2 | 0 | 4.5 | 32.6 | 43.6 | 0 | 0 | 0 | 48.9 |
| Vernonia cinerea Less | 0 | 8 | 23 | 0 | 8 | 32 | 22 | 0 | 0 | 0 | 57.5 |
| Joannesia princeps V. | 0 | 2.4 | 5.4 | 0 | 0 | 45.8 | 46.4 | 0 | 0 | 0 | 45.2 |
| Garcinia combogia D. | 0 | 0 | 2.3 | 0 | 38.3 | 57.9 | 0.8 | 0.4 | 0.3 | 0 | 61.5 |
| Garcinia indica Choisy | 0 | 0 | 2.5 | 0 | 56.4 | 39.4 | 1.7 | 0 | 0 | 0 | 65.2 |
| Illicium verum Hook | 0 | 4.4 | 0 | 0 | 7.9 | 63.2 | 24.4 | 0 | 0 | 0 | 50.7 |
| Melia azadirach Linn | 0 | 0.1 | 8.1 | 1.5 | 1.2 | 20.8 | 67.7 | 0 | 0 | 0 | 41.4 |
| Myristica malabarica L. | 0 | 39.2 | 13.3 | 0 | 2.4 | 44.1 | 1 | 0 | 0 | 0 | 61.8 |
| Urtica dioica Linn | 0 | 0 | 9 | 0 | 0 | 14.6 | 73.7 | 2.7 | 0 | 0 | 38.7 |
| Tectona grandis Linn | 0 | 0.2 | 11 | 0 | 10.2 | 29.5 | 46.4 | 0.4 | 0 | 0 | 48.3 |
| Canola | 0 | 0.1 | 5.2 | 0.2 | 2.5 | 58.1 | 28.1 | 0.4 | 1.6 | 0.4 | 55 |
| Lard | 0.1 | 1.9 | 24.5 | 2.8 | 14.4 | 38.3 | 13.4 | 0.3 | 0.7 | 0.1 | 63.6 |
| Yellow grease | 0 | 1.1 | 17.3 | 2.2 | 9.5 | 45.3 | 14.5 | 1.3 | 1.3 | 0 | 52.9 |
| Rape | 0 | 0 | 4.8 | 0 | 1.6 | 33 | 20.4 | 7.9 | 9.3 | 23 | 55 |
| Linseed | 0 | 0 | 5 | 0 | 2 | 20 | 18 | 55 | 0 | 0 | 52 |
| Wild mustard | 0 | 0.1 | 2.6 | 0.2 | 0.9 | 7.8 | 14.2 | 13 | 5.4 | 45.7 | 61.1 |
| Waste palm oil | 0 | 1 | 39 | 0.2 | 4.3 | 43.7 | 10.5 | 0.2 | 0.2 | 0 | 60.4 |
| Balanites roxburhii | 0 | 0 | 17 | 4.3 | 7.8 | 32.4 | 31.3 | 7.2 | 0 | 0 | 50.5 |
| Garcinia echinocarpa | 0 | 0 | 3.7 | 0 | 43.7 | 52.6 | 0 | 0 | 0 | 0 | 63.1 |
| Neolitsea umbrosa G. | 59.1 | 11.5 | 0 | 0 | 0 | 21 | 6.7 | 0 | 0 | 0 | 60.8 |
| Anamirta cocculus | 0 | 0 | 6.1 | 0 | 47.5 | 46.4 | 0 | 0 | 0 | 0 | 64.3 |
| Broussonetia p. Vent. | 0 | 0 | 4 | 0 | 6.1 | 14.8 | 71 | 1 | 0 | 0 | 41.2 |
| Salvadora oleoides D. | 35.6 | 50.7 | 4.5 | 0 | 0 | 8.3 | 0.1 | 0 | 0 | 0 | 66.1 |
| Nephelium L. | 0 | 0 | 0.2 | 0 | 13.8 | 45.3 | 0 | 0 | 4.2 | 0 | 64.9 |
| Ziziphus maurit. L. | 0 | 0 | 10.4 | 0 | 5.5 | 64.4 | 12.4 | 0 | 2.6 | 1.7 | 55.4 |
| Jajoba | 0 | 0 | 1.2 | 0 | 0 | 10.7 | 0.1 | 0.4 | 59.5 | 12.3 | 69 |
| Rape | 0 | 0 | 4.9 | 0 | 1.6 | 33 | 20.4 | 7.8 | 9.3 | 23 | 55 |
| Peanut | 0 | 0.1 | 8 | 0 | 1.8 | 53.3 | 28.4 | 0.3 | 2.4 | 0 | 53 |
| Grape | 0 | 0.1 | 6.9 | 0.1 | 4 | 19 | 69.1 | 0.3 | 0 | 0 | 48 |
| Sunflower | 0 | 0 | 6 | 0.1 | 2.9 | 17 | 74 | 0 | 0 | 0 | 49 |

The previous techniques provide a better result (DOE) is required for those techniques. If the techniques is applied with random dataset.

(scattered data), less accuracy will be achieved. Therefore, ANN give better result for random dataset.

Cascade neural network, in particular, is a neural network class that is analogous to feed-forward networks. Yet, the cascade neural network has a connection from the input as well as each preceding layer to following layers. In a network with three layers, for example, the output layer is directly connected with the input and hidden layer. Similar to feed-forward networks, a two or extra layer cascade neural network can learn the input-output relationship randomly well using sufficient hidden neurons. Cascade neural network can be utilised for any type of mapping from input to output. The benefit of this technique is that it contains the nonlinear input-output relationship by not disregarding such linear relationship. **Figure 2** shows the cascade neural networks architecture. The equation of cascade neural network is following Eq. 1.

Here, f^l and W_i^l are the activation function and weight from the input to the output layer, respectively. When there is an additional bias, Eq. 1 becomes Eq. 2.

$$y = \sum_{i=1}^n f^l W_i^l x_i + f^o \left(\sum_{j=1}^k W_j^o f_j^h \left(\sum_{i=1}^n W_{ji}^h x_i \right) \right) \quad (1)$$

$$y = \sum_{i=1}^n f^l W_i^l x_i + f^o \left(W^b + \sum_{j=1}^k W_j^o f_j^h \left(W_j^b + \sum_{i=1}^n W_{ji}^h x_i \right) \right) \quad (2)$$

In the present study, the data were distributed randomly by 70%, 15% and 15% for training, test and validation. Log-sigmoid (logsig) was set as the hidden layer transfer functions, whereas the linear (purelin) was set as the output layer. The flowchart of cascade neural network used in the present study is given in **Figure 3**.

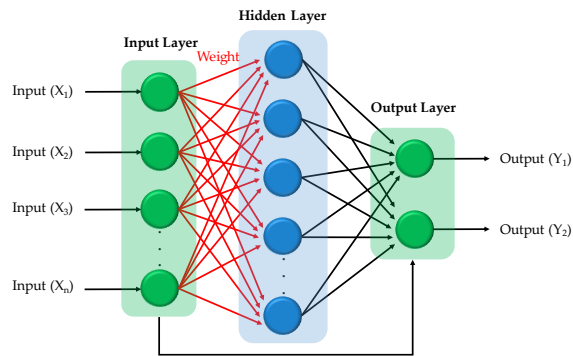


Figure 2. The general architecture of cascade neural networks

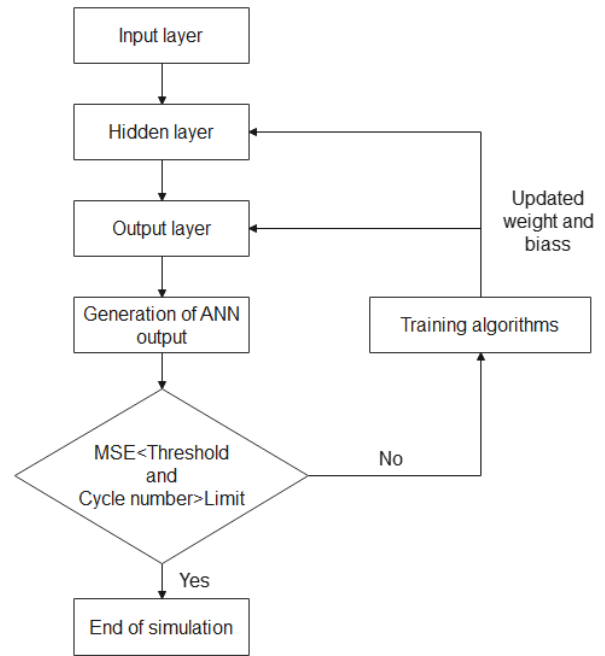


Figure 3. Flowchart of cascade network algorithm

3.3. Performance Criteria

Five different criteria were used; R, R², MAD, RMSE and MAPE to evaluate the prediction accuracy of each model using the following Eq. 3- Eq. 7.

Correlation Coefficient (R),

$$R = \sqrt{1 - \left\{ \frac{\sum_{i=1}^n (M_i - P_i)^2}{\sum_{i=1}^n P_i^2} \right\}} \quad (3)$$

Determination Coefficient (R²),

$$R^2 = 1 - \left\{ \frac{\sum_{i=1}^n (M_i - P_i)^2}{\sum_{i=1}^n P_i^2} \right\} \quad (4)$$

Mean Absolute Deviation (MAD),

$$MAD = \frac{1}{n} \sum_{i=1}^n |M_i - P_i| \quad (5)$$

Root Mean Squared Error (RMSE),

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (M_i - P_i)^2} \quad (6)$$

Mean Absolute Percentage Error (MAPE),

$$MAPE = \left\{ \frac{100}{n} \sum_{i=1}^n \left| \left(\frac{M_i - P_i}{M_i} \right) \right| \right\} \% \quad (7)$$

4. Results and Discussion

Figure 4 shows the coefficient of correlation (R) and determination (R²) for 10 different algorithms in cascade neural network examined in this study. R measures the association closeness of the points to a line of linear regression according to such points. Possible values of R varied from -1 to +1,

with -1 showing a perfectly linear inverse correlation and +1 showing that of positive correlation. Detailed R values of Cascade-LM algorithms for training, validation, test and all are presented in Figure 5. Moreover, the determination coefficient is a prediction criterion used to quantify how much variability of one particular factor can be triggered by its connection to another associated factor. The determination correlation is also known as the "goodness of fit," whose value ranging from 0 and 1, with value of 1 indicating a perfect fit, and is therefore a substantially reliable model for future predictions, while 0 indicating that the estimate does not accurately model the data at all.

The highest value of correlation and determination coefficient is given by Levenberg Marquardt algorithm. With an R value of 0.9615, LM algorithm signifies almost a perfectly linear positive correlation. Furthermore, the LM algorithm with a R² value of 0.9245 suggests that 92.45% of the dependent variable is predicted well

by the independent variable. On the contrary, the lowest value of correlation and determination coefficient is given by Gradient Descent with Momentum and Adaptive Learning Rate (GDx) with an R value of 0.7885 and R² of 0.6217.

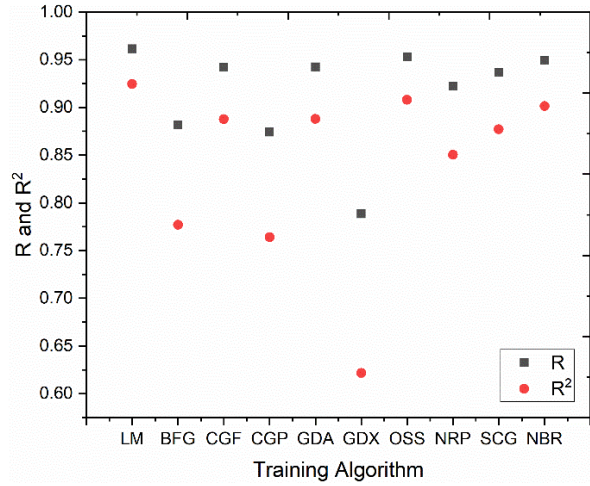


Figure 4. R and R² values for the ten investigated training algorithms

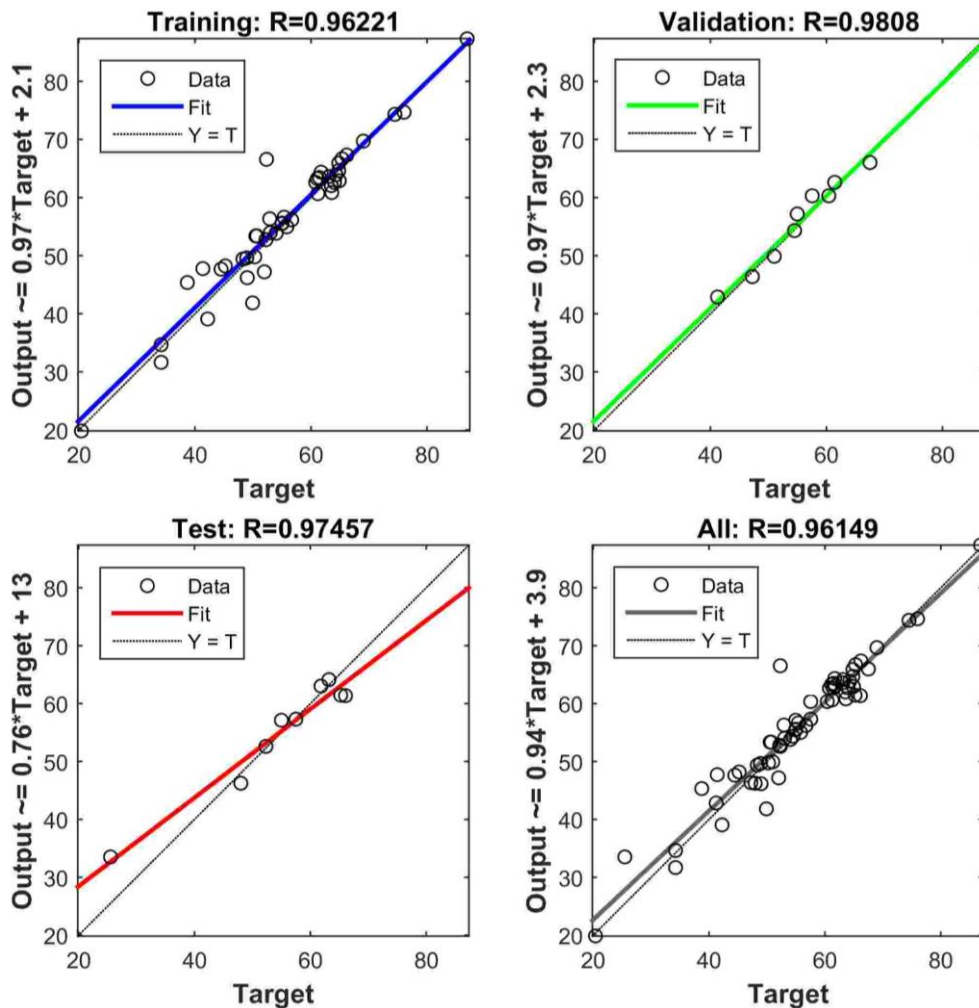


Figure 5. R values of Cascade-LM algorithms for training, validation, test and all

Figure 6 shows the value of MAD, RMSE and MAPE for all 10 training algorithms in cascade neural network examined in this study. MAD is a variability measure which denotes the average distance between examinations and their mean values. The term of the mean absolute deviation resonances to the standard deviation (SD). Both MAD and SD measure variability, but they have different calculations. Due to its relatively straightforward concept that better fits real life application, MAD is favoured to replace the standard deviation. Another method to evaluate how well a regression model fits a dataset is by calculating the RMSE. It is a metric that signify the average distance between the estimated values from the model and the real dataset values. The last prediction accuracy used in this study is MAPE. It measures a forecast system accuracy as a percentage. MAPE is considered as the most frequent measure used to predict error, working at its best when there are no extremes and no zeros.

The lowest value of MAD, RMSE and MAPE is given by Levenberg Marquardt algorithm, while that of the highest is given by Gradient Descent with Momentum and Adaptive Learning Rate (GDX). LM's lowest MAD value shows that data points bunching closer to its average value. Conversely, the highest MAD value of GDX indicates that the data points in Gradient Descent with Momentum and Adaptive Learning stretch further from the average values. LM's lowest RMSE value indicates the best prediction accuracy among of an Levenberg Marquardt among other investigated training algorithm to fit well a dataset. As far as the mean absolute percent error is concerned, the MAPE value of LM is 4.2971% meaning that the prediction is off by just over 4%. Note that since the MAPE is a percentage, it is far easier to comprehend its value compared to other accuracy measure.

Detailed results of R, R^2 , MAD, RMSE, and MAPE are provided in Table 2. Furthermore, the best results provided by Levenberg Marquardt algorithm is comprehensively provided in Figure 7 where actual and predicted CN for various test cases are presented. Looking at Table 2 and Figure 7, it is apparent that the LM and GDX training algorithm shows the best and the worst prediction accuracy, respectively.

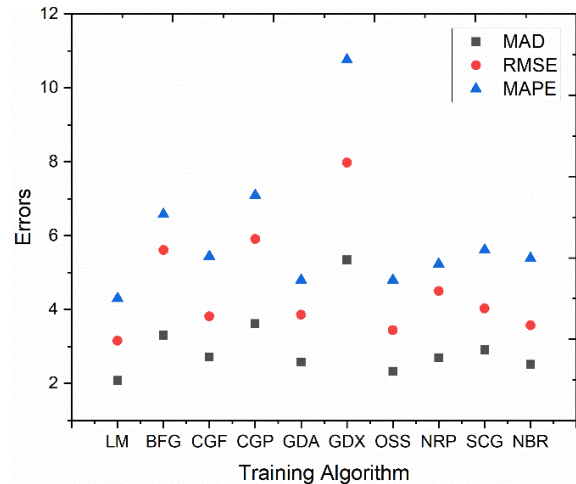


Figure 6. Errors for the ten investigated training algorithms

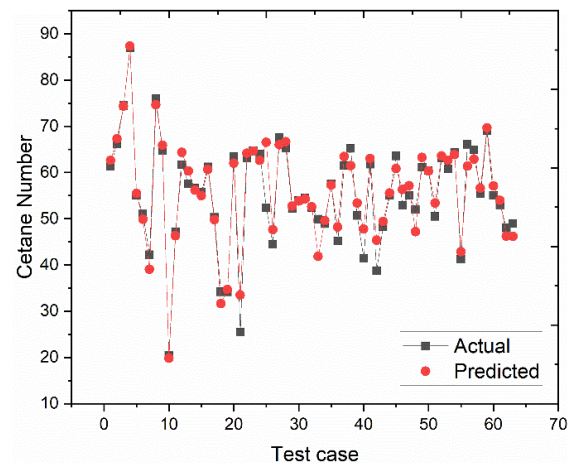


Figure 7. Actual and predicted CN for various test cases using Cascade Levenberg-Marquardt training algorithm

There are a number of explanations for the above results. Since there are two possible possibilities for the direction at every iteration, the LM is more robust. Levenberg Marquardt is also faster to converge than gradient descent. Moreover, LM is able to handle models with more than free parameters that are not exactly known. If the initial estimation is far-off from the mark, the LM algorithm is still able to discover the optimal solution. However, the Levenberg Marquardt may sometimes suffer from several drawbacks. For flat functions, the LM algorithm may become lost in parameter space. In several cases, such training algorithm can become exceptionally slow to converge. This is predominantly true when the model has more than ten parameters that needs the algorithm to move slowly along a closely well-defined crawl space.

Table 2. Performance evaluation of ANN models

| ANN training algorithm | R | R ² | MAD | MSE | RMSE | MAPE |
|------------------------|--------|----------------|--------|---------|--------|---------|
| Cascade-LM | 0.9615 | 0.9245 | 2.0804 | 9.9486 | 3.1541 | 4.2971 |
| Cascade-BFG | 0.8815 | 0.7770 | 3.3011 | 31.4749 | 5.6103 | 6.5837 |
| Cascade-CGF | 0.9422 | 0.8877 | 2.7139 | 14.5417 | 3.8134 | 5.4417 |
| Cascade-CGP | 0.8741 | 0.7641 | 3.6203 | 34.9113 | 5.9086 | 7.0998 |
| Cascade-GDA | 0.9423 | 0.8880 | 2.5798 | 14.9114 | 3.8615 | 4.7941 |
| Cascade-GDX | 0.7885 | 0.6217 | 5.3485 | 63.6301 | 7.9768 | 10.7621 |
| Cascade-OSS | 0.9528 | 0.9079 | 2.3282 | 11.8651 | 3.4446 | 4.7966 |
| Cascade-RP | 0.9222 | 0.8504 | 2.6972 | 20.2798 | 4.5033 | 5.2346 |
| Cascade-SCG | 0.9365 | 0.8771 | 2.9094 | 16.2064 | 4.0257 | 5.6135 |
| Cascade-BR | 0.9495 | 0.9015 | 2.5191 | 12.7715 | 3.5737 | 5.3889 |

5. Conclusion

In this study, a dataset of 63 samples of biodiesel was used to build an ANN model. To predict the CN of biodiesels in terms of their fatty acid methyl esters composition, 10 different ANN training algorithms using a 10-10-1 network structure were compared and analyzed. Results revealed that the ANN trained with Levenberg-Marquardt gave the highest accuracy. This model successfully predicted the CN of biodiesels with the highest correlation and determination coefficient ($R = 0.9615$, $R^2 = 0.9245$) as well as the lowest errors ($MAD = 2.0804$, $RMSE = 3.1541$, and $MAPE = 4.2971$).

CN determination by means of experimental work is a relatively expensive and laborious process. For that reason, developing accurate models for predicting biodiesel's CN from its FAME composition for various feedstocks would be beneficial. In the present study, we have shown that the Cascade neural network trained with the Levenberg-Marquardt algorithm using a 10-10-1 network structure was considered a promising alternative to the expensive experimental or empirical correlations for predicting biodiesel's CN. This promising alternative has a potential approach for further research by continuing the prediction model of CN with larger data.

Author's Declaration

Authors' contributions and responsibilities

The authors made substantial contributions to the conception and design of the study. The authors took responsibility for data analysis, interpretation and discussion of results. The authors read and approved the final manuscript.

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The authors declare no competing interest.

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